Balcombe C E (C) School



Maths Calculation Policy

Next Review:

Sep 2018

Before children move to written methods, they need:

- To understand the number system
- Know some number facts
- Have good mental strategies / mental agility
- Be confident in using concrete apparatus and pictorial representations to solve problems and explain their reasoning.

When children move to written methods they need to think

- What will the answer be roughly?
- Can I work it out in my head?
- What can I use to help me? Do I need a written method?
- · Does that answer my question?
- Does it make sense? Can I check?

Purpose of the Policy:

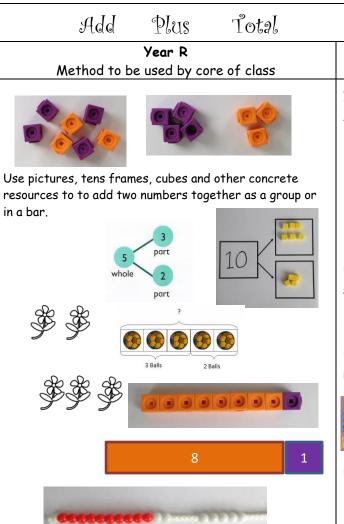
- To make teachers and parents aware of the strategies that pupils are formally taught within each year group that will support them to perform mental and written calculations. Pupils should not move on through the methods until they have secured and understood how to use the methods, including the concrete and pictorial representations.
- The policy supports teachers in identifying appropriate concrete apparatus and pictorial representations to help develop and secure
 understanding.

Aims of the policy:

- To ensure consistency and progression in our approach to calculation.
- To ensure that children develop an efficient, reliable, formal written method of calculation for all operations.
- To ensure that children can use these methods accurately with confidence and understanding.

How to use this policy:

- Use the policy as the basis of your planning but ensure you use previous or following years' guidance to allow for personalised learning.
- Always use Assessment for Learning to identify suitable next steps in calculation for groups of children.
- If, at any time, children are making significant errors, return to the previous stage in calculation.
- Always introduce a new concept/calculation using use suitable resources, models and images to support children's understanding of the calculation and place value, as appropriate.
- Encourage children to make sensible choices about the methods they use when solving problems.



See addition appendix 1- combining two parts to make a whole: part-whole model.

+ Addition +

Year 1

Method to be used by core of class

As year R plus:

Teach all the number bonds up to and including 10 and the related 'Fact Family' for each fact.

Use concrete objects to combine groups to add and solve missing number problems.

3+__= 10 Show this using the part/whole model.

Understand place value - can partition numbers and recombine numbers

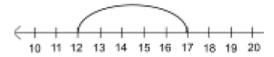








Usually start with the **biggest** number (if counting on) 12 + 5 = 17



Start at the larger number on the number line and count on in ones or in one jump to find the answer.

See addition appendix 1- combining two parts to make a whole: part-whole model. Appendix 2 starting at the bigger number and counting on.

More

Sum

Altogether

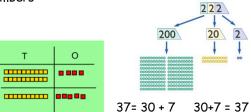
Year 2

Method to be used by core of class

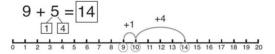
As year 1 plus:

Addition can be done in any order (commutative) 34 + 56 or 56 + 34

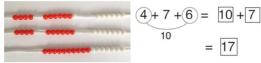
Understand place value - can partition numbers & recombine numbers



Use partitioning to add numbers, first with concrete apparatus, then as a possible mental method. Have a range of mental methods for calculating first with numbers to 20, then with numbers to 100 e.g. breaking numbers apart to use them flexibly, this may be with a bridging strategy (e.g. 7+5 could be thought of as 7+3+2 or 5+5+2), a compensating strategy (e.g. 7+9 could be thought of as 7+10 then -1) or by using a near double (e.g. 7+8 =14+1).



Learn to add three numbers 4 + 7 + 6 = 17Put 4 and 6 together to make 10. Add on 7.



Use number bonds e.g. 4+6=10 to work out 40+60=100

See addition appendix 2 starting at the bigger number and counting on. Appendix 3 regrouping to make 10. Appendix 4 adding three single digits.

+ Addition + Plas Total Add Altogether More Sum Year 5 Year 6 Year 3 Year 4 Method to be used by core of class Method to be used by core of class Method to be used by core Method to be used by core of of class class As year 2 plus: As year 4 plus: As year 5 plus: As year 3 plus: Compact addition involving large Understand place value - can partition numbers & Add ones, tens and hundreds to a three-digit number Compact addition with numbers recombine numbers to Children can draw a pictoral representation of the larger than four digits. Compact addition with decimals to support column addition. columns and place value counters to further support Compact addition with decimals their learning and understanding. three places. to two places. e.g. e.g. 32.756 32.75 24 + 15= +48.646 +48.64 Add together the ones first then add the tens. 81,402 81.39 Use the Base 10 blocks first before moving onto 11 11 7 11 1 5 place value counters. • Expanded addition, TU then TU crossing tens 24.5+ 36.238 2 3 . 3 6 Compact addition (integers only) with numbers up to barriers, then HTU (three digits) four digits 34 + 62= 5 9 . 7 7 0 24 500 146 30 + 4+36.238 + 527 e.q. 60 + 260,738 7648 90 + 6 = 96+ 1486 9134 See addition appendix 5 column See addition appendix 5 column 494 + 368 = 111 method- no regrouping and 400 + 90 + 4 method- no regrouping and appendix appendix 6 column method -6 column method - regrouping 300 + 60 + 8 Expanded addition may be used for decimals in real regrouping (bridging ten) 700 +150 +12 =862 contexts e.g. money and length. (bridging ten) then Compact addition f.11.35+ f.12.43= 494 £10 + £1 + 30p + 5p + +368 £10 + £2 + 40p + 3p862 £20 + £3 + 70p + 8p = £23.7811 See addition appendix 5 column method- no See addition appendix 5 column method- no regrouping and appendix 6 column method regrouping and appendix 6 column method regrouping (bridging ten) regrouping (bridging ten)

Subtract

take away

less than

- Subtraction -

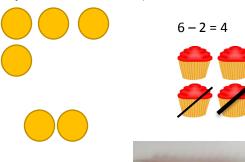
ทเ้ทแร

difference between

Year R

Method to be used by core of class

Use physical objects, counters, cubes etc to show how objects can be taken away.







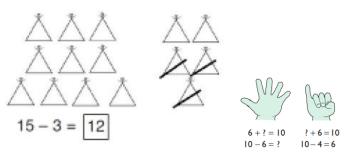
Use counters and bead strings, move them away from the group as you take them away counting backwards as you go.

See subtraction appendix 1 taking away ones and appendix 2 counting back.

Year 1

Method to be used by core of class

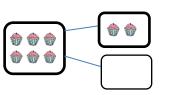
As year R plus:

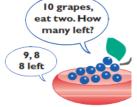


Understand that subtraction can be seen as taking away and finding the difference. Use the part-whole model to take away.

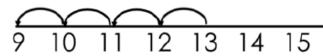


The difference between 11 and 14 is 3.





First with concrete apparatus, then number line or 100 square, then mentally. Count back on a number line or number track when secure with concrete apparatus.



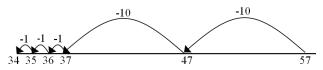
See subtraction appendix 1 taking away ones, appendix 2 counting back, appendix 3 finding the difference and appendix 4 part-whole model.

Year 2

Method to be used by core of class

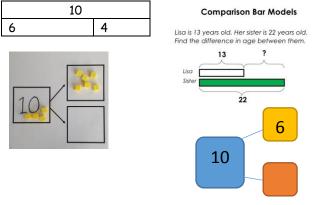
As year 1 plus:

Subtract using concrete objects such as Numcion, make the whole and take away the correct amount. Then progress to pictorial representations and mental methods. Start at the bigger number and count back the smaller number showing the jumps on the number line.



This can progress all the way to counting back using two 2 digit numbers.

No. bonds to 100 (at least with multiples of 10). Understand the number line as a continuum. Understand that subtraction is the inverse of addition (Numicon is a particularly useful image) and bar model.



See subtraction appendix 2 counting back, appendix 3 finding the difference and appendix 4 part-whole model and appendix 5 make 10.

Subtract

take away

less than

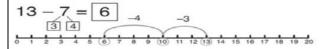
- Subtraction - minus

difference between

Year 3

Method to be used by core of class

As year 2 plus:

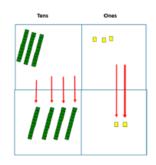


Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.

Number line method (2 and 3 digit numbers) 351-165=186



Begin expanded subtraction using concrete objects and pictorial representations.





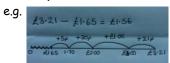
See subtraction appendix 5 make 10. Appendix 6 column method without regrouping.

Year 4

Method to be used by core of class

As year 3 plus:

Number line method (2, 3, 4 digit numbers, extending to decimals in a real context)



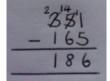
Expanded subtraction

e.g. 354 - 165

100	10	•	<u>Calculations</u>
100	<u>⊚</u> ⊗⊗.≫		176 - 64 = 176 - <u>64</u> <u>112</u>

Use base 10 or place value counters alongside the written calculation to help to show working.

Compact subtraction



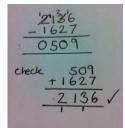
See subtraction appendix 5 make 10. Appendix 6 column method without regrouping.

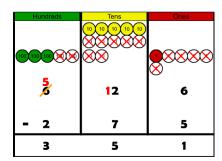
Year 5

Method to be used by core of class

As year 4 plus:

Compact subtraction, involving numbers larger than 4 digits and with decimals to 2 places.





Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make. When confident children can find their own way to record the exchange/regrouping.

See subtraction appendix 5 make 10. Appendix 6 column method without regrouping.

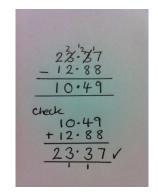
Year 6

Method to be used by core of class

As year 5 plus:

Compact subtraction involving large numbers.

Compact subtraction with decimals up to three places.



See subtraction appendix 5 make 10. Appendix 6 column method without regrouping.

x Multiplication x Multiply Lots of groups of multiple of product times Year R Year 2 Year 1 Method to be used by core of class Method to be used by core of class Method to be used by core of class Introduce language and concept of making equal As Year 1 plus: As year R plus: By the end of the year pupils should recall all multiplication facts groups. Recall doubles to 10. Use this knowledge to support halving Begin to double numbers to 5. Use concrete for the 2, 5 and 10 times tables. and doubling larger numbers. apparatus to show how to double a number. Understand multiplication as scaling. 16 The giant is twice as big as a boy. Double 4 is 8 12 $8 \div 2 = 4$ 20 Understand multiplication as repeated addition. Understand that multiplication is commutative (arrays eq. Numicon and Cuisenaire particularly useful). 5+5+5+5+5+5=30 $5 \times 6 = 30$ See multiplication appendix 1 doubling. 5 multiplied by 6 6 groups of 5 6 hops of 5 Understand that multiplication and division are the inverse of each other. $4 \times 10 = 40$ 10×4=40 40÷4=10 Group sets of objects reliably in 2s, 5s and 10s. 40÷10=4 Recognise number sequences e.g. 2s, 5s and 10s. Use of arrays See multiplication appendix 2 counting in multiples. Appendix 3 repeated addition. Appendix 4 arrays- showing commutative multiplication. See multiplication appendix 1 doubling. Appendix 2 counting in multiples. Appendix 3 repeated addition. Appendix 4 arrays- showing commutative multiplication.

Multiply

times

lots of

x Multiplication x groups of

multiple of

product

Year 3

Method to be used by core of class

As year 2 plus:

Focus on understanding, representing and remembering times tables facts for 2,5,10,3,4 and 8 times tables, including division facts



4x8=32.8x4=32.32÷4=8.32÷8=4

Note - before moving to any TU x U, the children will need be able to multiply a multiple of 10 by a single digit (T0xU) Numicon or Cuisenaire in the grid e.g. 20x4, 40x5

See multiplication appendix 4 arraysshowing commutative multiplication. Appendix 5 grid method.

Year 4

Method to be used by core of class

As year 3 plus:

ALL times tables facts to 12 x 12 should be known by end of year 4 including multiplying by 0 and 1. Children should learn to multiply three numbers together.

$$4 \times 6 \times 3 =$$

 $4 \times 6 = 24 \times 3 = 72$

Grid method TU x U or HTU X U Show the link with arrays to first introduce the grid method. e.g. 4×13

х	10	3
4		

e.a. 7 x 39

×	30	9	Total
7	210	63	273

(but know when to calculate mentally e.g. x2, x10, x5)

e.a. 245 x 6

X	200	40	5	Tot al
6	120 0	24 0	30	147 0

See multiplication appendix 4 arraysshowing commutative multiplication. Appendix 5 grid method.

Year 5

Method to be used by core of class

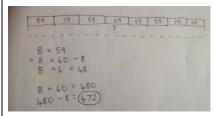
As year 4 plus:

Multiply with numbers up to 4 digits. Grid Method for TU x TU, HTU x TU, THTU x TU or U.

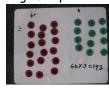
ea 35 x 46

×	30	5	Tot
			αl
40	1200	200	140
			0
6	180	30	
			<u>210</u>
То			<u>161</u>
tal			<u>0</u>

Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written method.



Long Multiplication (expanded)



35	
x 46	
30	
200	
1200	
1610	

See multiplication appendix 4 arrays- showing commutative multiplication. Appendix 5 grid method. Appendix 6 column multiplication.

Year 6

Method to be used by core of class

As year 5 plus:

Long Multiplication

Up to 4 digit x 2 digit



Moving to... Decimal numbers to 2 places multiplied by whole numbers

Note -some children may continue to use the grid method

If it helps, children can write out what they are solving next to their answer.

See multiplication appendix 4 arraysshowing commutative multiplication. Appendix 5 grid method. Appendix 6 column multiplication.

Division ÷ Share equally group equally divide remainder factor quotient Year 1 Year R Year 2 Method to be used by core of class Method to be used by core of class Method to be used by core of class Introduce language and concept of Understand division as sharing equally into groups. As Year 1 plus: By the end of the year pupils should recall all division facts for the 2,5 sharing fairly and making equal Share into groups using concrete apparatus then move to pictorial representations. and 10 times tables. groups. How many 3s shared between 5 000000000000000 5 hops in 15. How big is each hop? $15 \div 5 = 3$ Link division to multiplication by creating an array and thinking about the number Know multiplication facts (including the related 'fact family' sentences that can be created. e.g 3x5=15, 5x3=15, 15÷3=5, 15÷5=3) Eq $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$ 3x5=15 $15\div5=3$ Finding remainers: Divide objects between groups and see how much is left 5x3=15 15÷3=5 over $14 \div 3 =$ $(\underbrace{\bullet})(\underbrace{\bullet})(\underbrace{\bullet})(\underbrace{\bullet})_{\text{remainded}}$ Finding half and quarter using the same methods. See division appendix 1 sharing objects into groups. Appendix 2 division as grouping. Appendix 3 division within arrays. See division appendix 1 sharing objects into groups. Appendix 2 division as grouping. Appendix 3 division within arrays. Appendix 4 division with a remainder.

Share equally

group equally

divide

Division ÷

remainder

factor

quotient

Year 3

Agreed method to be used by core of class

As year 2 plus:

Focus on understanding, representing and remembering times tables facts for 2, 5, 10, 3, 4 and 8 times tables, including division facts.

e.g



4x8=32, 8x4=32, 32÷4=8, 32÷8=4

See division appendix 3 division within arrays. Appendix 4 division with a remainder.

Year 4

Agreed method to be used by core of class

As year 3 plus:

Focus on understanding, representing and remembering times tables facts for ALL times tables up to 12 x12 including division facts.

It is especially important that children understand that division can be grouping or sharing.

e.g. 12÷3=4

12 sweets between 3 people gives 4 sweets each.







(3 groups of 4)

'How many 3s in 12?' gives 4 groups of 3

See division appendix 3 division within arrays. Appendix 4 division with a remainder.

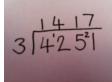
Year 5

Agreed method to be used by core of class

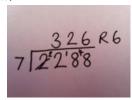
As year 4 plus:

Short division, up to 4 digit numbers divided by 1 digit numbers

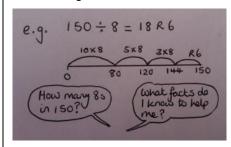
e.g. 4251÷3



Including dealing with remainders in context.



Or...Chunking on a number line



Multiply and divide whole numbers and those involving decimals by 10, 100 and 1000.

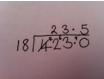
See division appendix 3 division within arrays. Appendix 4 division with a remainder. Appendix 5 short division.

Year 6

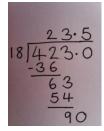
Agreed method to be used by core of class

As year 5 plus:

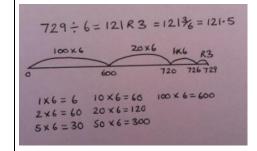
Short division, up to 4 digit numbers divided by 1 or 2 digit numbers e.g. $423 \div 18$



or Long division



Or Chunking on a number line



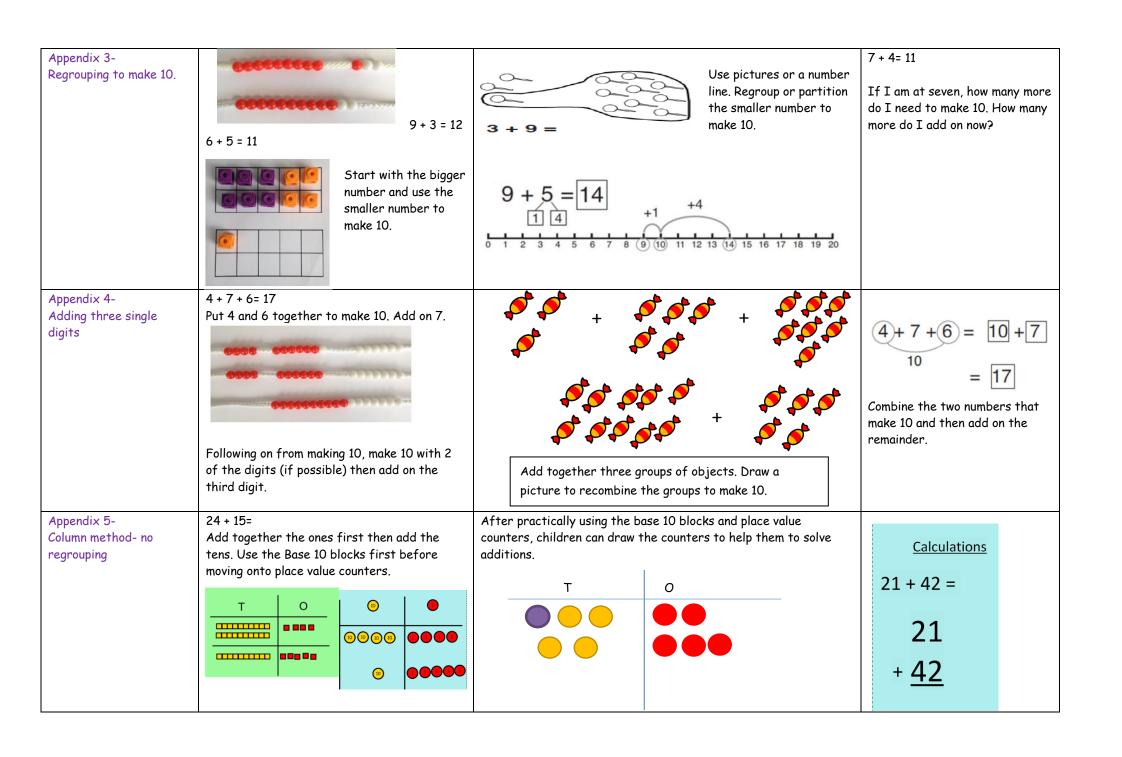
See division appendix 3 division within arrays. Appendix 4 division with a remainder. Appendix 5 short division.

Appendix

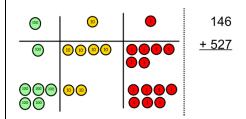
Progression in calculations linked to concrete apparatus, pictorial representations and abstract methods. When introducing a new method of calculation the concrete apparatus should be used first. Once this is secure pupils can then be moved onto pictorial representations and then abstract methods.

Addition:

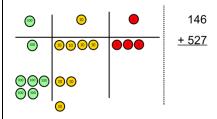
Objective and	Concrete	Pictorial	Abstract
Strategies			
Appendix 1- Combining two parts to make a whole: part- whole model	Use cubes to add two numbers together as a group or in a bar.	John Spart Whole 2 part Use pictures to add two numbers together as a group or in a bar.	4 + 3 = 7 10= 6 + 4 5 Use the part-part whole diagram as shown above to move into the abstract.
Appendix 2- Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	12 + 5 = 17 10 11 12 13 14 15 16 17 18 19 20 Start at the larger number on the number line and count on in ones or in one jump to find the answer.	5 + 12 = 17 Place the larger number in your head and count on the smaller number to find your answer.



Appendix 6-Column methodregrouping (bridging 10) Make both numbers on a place value grid.



Add up the units and exchange 10 ones for one 10.

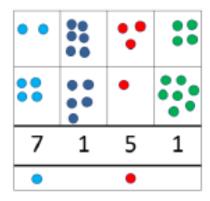


Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

As children move on to decimals, money and decimal place value counters can be used to support learning.

Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.



Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

$$\begin{array}{rrrr} 20 & + & 5 \\ \underline{40} & + & 8 \\ 60 & + & 13 & = 73 \end{array}$$

As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here. $\frac{+85}{621}$

536

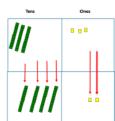
Subtraction:

Objective and Strategies	Concrete	Pictorial	Abstract
Appendix 1- Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. 6 - 2 = 4	Cross out drawn objects to show what has been taken away.	18 - 3 = 15 8 - 2 = 6
Appendix 2- Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 - 4 Use counters and move them away from the group as you take them away counting backwards as you go.	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line. -10 -10 -10 -10 -10 -10 -10 -10 -10 -1	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.

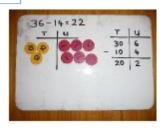
Appendix 3-	Compare amounts and objects to find the		Hannah has 23 sandwiches,
Find the difference	difference.	+6 Count on to	Helen has 15 sandwiches. Find
		find the	the difference between the
		difference.	number of sandwiches.
	Use cubes to build		
	towers or make	0 1 2 3 4 5 6 7 8 9 10 11 12	
	bars to find the		
	difference		
	12	Comparison Bar Models	
	Use basic bar	Draw bars to Lisa is 13 years old. Her sister is 22 years old.	
	models with	find the Find the difference in age between them.	
	items to find	difference 13 ?	
	the difference	between 2	
		numbers. Lisa Sister	
	3 Erasers ?	313161	
		22	
Appendix 4	Link to addition- use the	Use a pictorial representation of objects to show the part whole	
Part- Whole Model	part whole model to help	model.	5
	explain the inverse		
	between addition and		10
	subtraction.		
	7540 : 11 14		
	If 10 is the whole and 6		
	is one of the parts. What is the other part?		Move to using numbers within
	10 - 6 =		the part whole model.
Appendix 5-	14 - 9 =		
Make 10		13 - 7 = 6	16 - 8 =
	0000 0000 0000	13 4 -3	
		0 1 2 3 4 5 (6) 7 8 9 (10) 11 12 (13) 14 15 16 17 18 19 20	How many do we take off to
		0 1 2 3 4 0 0 7 0 0 10 11 12 13 14 13 10 17 10 18 23	reach the next 10?
		Start at 13. Take away 3 to reach 10. Then take away the	
	Make 14 on the ten frame. Take away the four	remaining 4 so you have taken away 7 altogether. You have	How many do we have left to
	first to make 10 and then takeaway one more	reached your answer.	take off?
	so you have taken away 5. You are left with	, '	
	the answer of 9.		

Appendix 6-Column method without regrouping

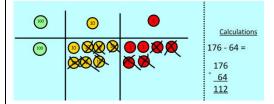
Use Base 10 to make the bigger number then take the smaller number away.



Show how you partition numbers to subtract. Again make the larger number first.



Calculations 4444



Draw the Base 10 or place value counters alongside the written calculation to help to show working.

47-24=23 40+7 -20+4

This will lead to a clear written column subtraction



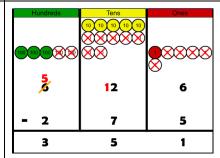
Appendix 7-Column method with regrouping

Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

Make the larger number with the place value counters

100	10	•	<u>Calculations</u>
(ii) (iii)	10 (10 (10	0 0 0	234 - 88

Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.



When confident, children can find their own way to record the exchange/regrouping. Just writing the numbers as shown

here shows that the child

understands the method and knows

when to exchange/regroup.

Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.

Children can start their formal written method by partitioning the number into clear place

836-254=582

200 50 4

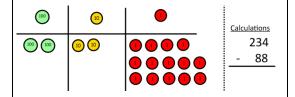
value columns.

500 80 2

728-582=146 °7 '2 8 8 2

Moving forward the children use a more compact method.

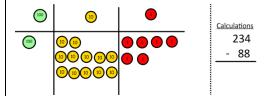




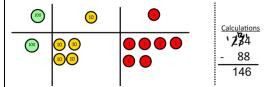
Now I can subtract my ones.

	100	10	•	<u>Calculations</u>
•	000 100	(i) (ii)		234 <u>- 88</u>

Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



Now I can take away eight tens and complete my subtraction



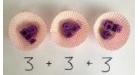
Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.

This will lead to an understanding of subtracting any number including decimals.

Multiplication

Objective and Strategies	Concrete	Pictorial	Abstract
Appendix 1- Doubling	Use practical activities to show how to double a number. $double \ 4 is \ 8 \\ 4 \times 2 = 8$	Draw pictures to show how to double a number. Double 4 is 8	16 10 6 12 20 12 Partition a number and then double each part before recombining it back together.
Appendix 2- Counting in multiples	Count in multiples supported by concrete objects in equal groups.	Use a number line or pictures to continue support in counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30

Appendix 3-Repeated addition





There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?



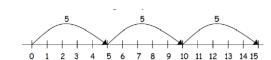


2 add 2 add 2 equals 6

Write addition sentences to describe objects and pictures.



Use different objects to add equal groups.



5 + 5 + 5 = 15



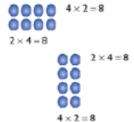
Appendix 4-Arrays- showing commutative multiplication

Create arrays using counters/ cubes to show multiplication sentences.





Draw arrays in different rotations to find **commutative** multiplication sentences.



Link arrays to area of rectangles.

Use an array to write multiplication sentences and reinforce repeated addition.



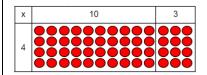
$$5 + 5 + 5 = 15$$

$$3 + 3 + 3 + 3 + 3 = 15$$

$$5 \times 3 = 15$$

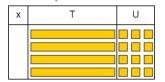
$$3 \times 5 = 15$$

Appendix 5-Grid Method Show the link with arrays to first introduce the grid method.



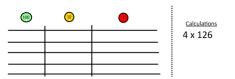
4 rows of 10 4 rows of

Move on to using Base 10 to move towards a more compact method.

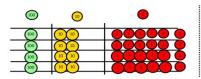


4 rows of 13

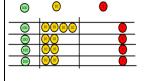
Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.



Fill each row with 126.



Add up each column, starting with the ones making any exchanges needed.

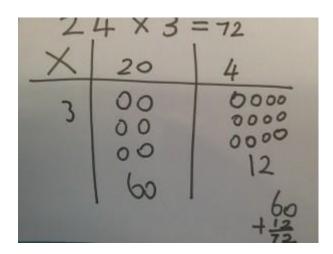


Calculations
4 x 126

Then you have your answer.

Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.

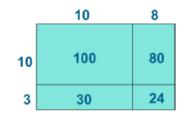


Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

$$210 + 35 = 245$$

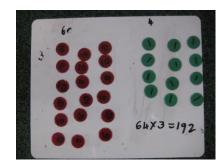
Moving forward, multiply by a 2 digit number showing the different rows within the grid method.



Х	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

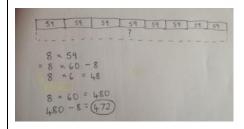
Appendix 6Column multiplication

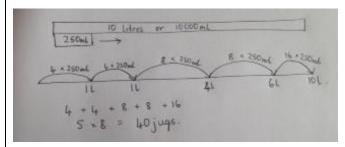
Children can continue to be supported by place value counters at the stage of multiplication.



It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.

Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.





Start with long multiplication, reminding the children about lining up their numbers clearly in columns.

If it helps, children can write out what they are solving next to their answer.

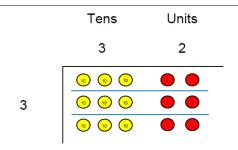
This moves to the more compact method.

Division

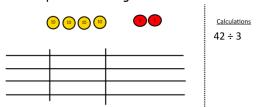
Objective and Strategies	Concrete	Pictorial	Abstract
Appendix 1- Sharing objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$	Share 9 buns between three people. 9 ÷ 3 = 3
Appendix 2- Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	Use a number line to show jumps in groups. The number of jumps equals the number of groups. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?

Appendix 3- Division within arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created.		Find the inverse of multiplication and division sentences by creating four linking number sentences. 7 × 4 = 28 4 × 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7
	Eg 15 ÷ 3 = 5	Draw an array and use lines to split the array into groups to make multiplication and division sentences.	
Appendix 4- Division with a remainder	14 ÷ 3 = Divide objects between groups and see how much is left over	Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.	Complete written divisions and show the remainder using r.
		Draw dots and group them to divide an amount and clearly show a remainder.	$\begin{array}{c} 29 \div 8 = 3 \text{ REMAINDER 5} \\ \uparrow \uparrow \uparrow \\ \text{dividend divisor quotient} \end{array}$ remainder
		emainder 2	

Appendix 5-Short division



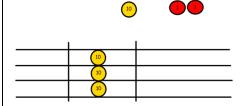
Use place value counters to divide using the bus stop method alongside



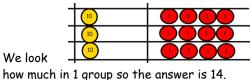
42 ÷ 3=

We look

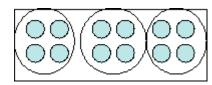
Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.



We exchange this ten for ten ones and then share the ones equally among the groups.



Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.



Encourage them to move towards counting in multiples to divide more efficiently.

Begin with divisions that divide equally with no remainder.

Move onto divisions with a

Finally move into decimal places to divide the total accurately.